



fracture mechanics of composites

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FRACTURE MECHANICS OF COMPOSITES

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Foreword

The Symposium on Fracture Mechanics of Composites was held at the National Bureau of Standards, Gaithersburg, Md., on 25 Sept. 1975. ASTM Committee D-30 on High Modulus Fibers and Their Composites sponsored the symposium. G. P. Sendeckyj, Air Force Flight Dynamics Laboratory, presided as the symposium chairman.

Related ASTM Publications

Composite Materials: Testing and Design, STP 546 (1974), \$39.75,
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Applications of Composite Materials, STP 524 (1973), \$16.75,
04-524000-33

Analysis of the Test Methods for High Modulus Fibers and Composites,
STP 521 (1973), \$30.75, 04-521000-33

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This publication is made possible by the authors and, also, the unheralded efforts of the reviewers. This body of technical experts whose dedication, sacrifice of time and effort, and collective wisdom in reviewing the papers must be acknowledged. The quality level of ASTM publications is a direct function of their respected opinions. On behalf of ASTM we acknowledge with appreciation their contribution.

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